Feel free to work with other students on these problems. However all written work should be your own. Also, be sure to give written credit, on the assignment, for any ideas you get from other people.

All proofs should be as short and clear as possible. If you deviate from the style of proof given in the notes you should only do so consciously and for good reason.

Exercise 8.1. For all $p, q \in \mathbb{Q}$, if $p < q$ then $p < (p+q)/2 < q$.

Exercise 8.2 (Archimedean Property for $\mathbb{Q}$). For all $p, q \in \mathbb{Q}$, if $0 < p < q$ then there is a natural number $n \in \mathbb{N}$ so that $q < np$.

Exercise 8.3. Prove directly from the definitions that for all $x, y \in \mathbb{R}$, if $x <_\mathbb{R} y$ then there is a rational number r so that $x <_\mathbb{R} E(r) <_\mathbb{R} y$.

Exercise 8.4. Prove directly from the definitions that for all $x \in \mathbb{R}$, either $0_\mathbb{R} = |x|$ or $0_\mathbb{R} <_\mathbb{R} |x|$.