

Please let me know if any of the problems are unclear or have typos.

**Exercise 3.1.** Suppose that  $\alpha \subset F^2$  is a simple closed curve. Show that  $\alpha = 1 \in \pi_1(F)$  if and only if  $\alpha$  bounds a disk in  $F$ .

**Exercise 3.2.** [Medium] Suppose that  $F^2 \subset S^3$  is smoothly embedded, connected and without boundary. Prove that if  $F$  is not a sphere then  $F$  compresses. [Idea: rewrite the proof of Alexander's theorem.]

**Exercise 3.3.** [Jordan-Brouwer separation] Suppose that  $F^2 \subset S^3$  is smoothly embedded, connected and without boundary. Show that  $F$  separates  $S^3$ . Deduce that  $F$  is two-sided. Deduce that  $F$  is orientable.

**Exercise 3.4.** Prove that every smoothly embedded two-torus  $T^2 \subset S^3$  bounds a solid torus ( $D^2 \times S^1$ ) on at least one side. Find an embedded  $S_2$  in  $S^3$  that does not bound a handlebody on either side.

**Exercise 3.5.** Suppose that  $\rho: M' \rightarrow M^3$  is a covering map. Show that if  $M'$  is irreducible then  $M$  is as well.

**Exercise 3.6.** Suppose that  $\rho: M' \rightarrow M^3$  is a covering map. Suppose that  $F \subset M$  is an properly embedded surface. Show that if  $F' = \rho^{-1}(F)$  is incompressible then  $F$  is as well.

**Exercise 3.7.** [Hard] Show that all  $I$ -bundles over  $S^2$  are equivalent. Find infinitely many inequivalent  $S^1$ -bundles over  $S^2$ .