

Please let me know if any of the problems are unclear or have typos.

**Exercise 6.1.** Suppose  $F$  is a *wallpaper orbifold*:  $F$  is closed and  $\chi^{\text{orb}}(F) = 0$ . Show  $F$  is finitely covered by  $\mathbb{T}^2$  and thus  $F$  is good.

**Exercise 6.2.** Show the teardrop and spindle orbifolds are bad. [This is the easy direction of Theorem 2.3 of Scott's article.]

**Exercise 6.3.** [Medium] Suppose  $\rho: F \rightarrow E$  and  $\sigma: G \rightarrow E$  are orbifold covering maps. Show that there is an orbifold  $H$  having a pair of orbifold covering maps  $\tau: H \rightarrow F$  and  $v: H \rightarrow G$ .

**Exercise 6.4.** Suppose  $\rho: F \rightarrow E$  is an orbifold covering. Show that  $F$  is good if and only if  $E$  is good.

**Exercise 6.5.** [Very hard] Suppose  $F$  is a compact good two-orbifold. Give a direct topological proof that there is a orbifold covering  $\rho: E \rightarrow F$ , with  $E$  a surface, where  $\rho$  has finite degree. [This is Theorem 2.5 from Scott's article.]

**Exercise 6.6.** [Reading] Review the statement of the uniformization theorem for surfaces. Using Exercise 6.5, prove if  $F$  is a closed good orbifold then  $F$  admits a geometric structure modelled on one of  $\mathbb{S}^2$ ,  $\mathbb{E}^2$ , or  $\mathbb{H}^2$ . [This is Theorem 2.4 from Scott's article. The development here is a bit different!]

**Exercise 6.7.** Compute presentations for  $\pi_1^{\text{orb}}(F)$  as  $F$  ranges over the wallpaper orbifolds.

**Exercise 6.8.** Compute presentations for  $G = \pi_1^{\text{orb}}(S^2(p, q, r))$  and  $H = \pi_1^{\text{orb}}(D^2(\bar{p}, \bar{q}, \bar{r}))$ . Recall that there is a two-fold covering map  $\rho: S^2(p, q, r) \rightarrow D^2(\bar{p}, \bar{q}, \bar{r})$ . Describe how  $\rho_*: G \rightarrow H$  transforms the generators; show that the image is index two.